## Voltage-Induced Dependence of Raman-Active Modes in Single-Wall Carbon Nanotube Thin Films

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## ABSTRACT

8 We report on electrical Raman measurements in transparent and conducting single-wall carbon nanotube (SWNT) thin films. Application of 9 external voltage results in downshifts of the D and G modes and in reduction of their intensity. The intensities of the radial breathing modes 10 increase with external electric field related to the application of the external voltage in metallic SWNTs, while decreasing in semiconducting 11 SWNTs. A model explaining the phenomenon in terms of both direct and indirect (Joule heating) effects of the field is proposed. Our work 12 rules out the elimination of large amounts of metallic SWNTs in thin film transistors using high field pulses. Our results support the existence 13 of Kohn anomalies in the Raman-active optical branches of metallic graphitic materials.

Transparent and conducting single-wall carbon nanotube 15 (SWNT) thin films are two-dimensional, low-density net-16 works of SWNTs<sup>1</sup> which are interesting both fundamentally 17 and technologically. Recently, it has been noticed<sup>2</sup> that the 18 Drude relaxation times in SWNT thin films, and therefore 19 20 their optolectronic properties, are controlled by intertube processes. This is an important difference with respect to 2122individual SWNTs where intratube processes dominate.3 The intertube processes in SWNT thin films arise from the tube 23to tube transport because the distance between the electrodes 24  $(\sim 20 \ \mu m)$  is typically much larger than the SWNT length. 25 26The transport properties in these networks can be explained by the percolation theory.<sup>1</sup> 27

28Technologically, the ability to tailor the optical absorption coefficient and conductivity of SWNT thin films over several 29 orders of magnitude makes them attractive for transparent 30 and flexible electronics.<sup>4–7</sup> During SWNT thin film transistor 31fabrication, it is a common practice to precondition the 32 SWNT network using high voltage pulses to improve the 33 on/off ratio through supposed preferential elimination of 34 metallic SWNTs by Joule heating.<sup>4-7</sup> This effect is claimed 35on the basis of the decrease in channel conductivity and a 36 37 similar effect occurring in individual SWNTs, but little information on the modifications of the SWNTs in thin films 38 after voltage application is available and a Raman study is 39 40 still lacking.

In this Letter, we report on the Raman measurements of SWNT thin films recorded under external voltages. We have found that, although the conductivity strongly decreases, the changes in the Raman peaks are to the largest extent reversible. The films were deposited on glass using the

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method of Wu et al.<sup>8</sup> from 10, 30, and 50 mL of a 2 mg/L 46 suspension of purified HiPCO SWNTs.<sup>2,9</sup> Gold electrodes 47 (width 1 mm, distances 20 and 60  $\mu$ m) were defined on each 48 substrate. External voltages of 0-15 V (leading to electric 49 fields  $E_{\text{ext}} = 0-7500 \text{ V cm}^{-1}$ ) were applied during the 50Raman measurements using a GW GPS-1850D power 51 supply. The spectra were recorded in air on a Renishaw InVia 52spectrometer. Our setup for electrical Raman measurements 53 is presented in Figure 1a. Low laser powers (12.5  $\mu$ W/ $\mu$ m<sup>2</sup> 54at 1.96 eV excitation, 25  $\mu$ W/ $\mu$ m<sup>2</sup> at 1.57 eV) were used 55and tested to not produce laser heating. The current was 56simultaneously monitored using a Keithley 195A multimeter. 57Each series of Raman spectra at the varying voltage was 58 recorded on the same spot in order to attain comparable 59 signal intensity. After any measurment at a given external 60 field, sufficiently low field (500 V/cm, leading to undetect-61 able changes in the Raman signal) was applied so that a low-62 field Raman spectrum and the sample conductance could be 63 recorded. 64

The typical variation of the G-bands<sup>3</sup> and the doubly 65 resonant D-band<sup>10</sup> under the influence of an electric field 66 are shown in parts b and c of Figure 1, respectively. A clear 67 decrease in peak position ( $\Omega$ ) and intensity ( $I_S$ ) for both bands 68 with increasing electric field  $(E_{ext})$  can be observed. Similar 69 shifts in the Raman bands under the influence of electric 70fields have been observed in ferroelectrics.<sup>11</sup> In contrast, 71 electrochemical Raman measurements of SWNT electrodes 72 in aqueous environments<sup>12</sup> resulted in upshifts of the G-73 bands, which clearly points to differences between our and 74 such experiments. Electromechanical Raman measurements 75may lead to both upshifts or downshifts.<sup>13</sup> 76



**Figure 1.** (a) Schematic of the setup for electrical Raman measurements. Typical dependence of the Raman modes on the electric field ( $E_{ext}$ ) (b) for the G peak (excitation energy  $\hbar \omega = 1.96$  eV) and (c) for the D peak. From panels b and c, the two main effects, peak downshifts and decrease in peak intensities, are evident.



**Figure 2.** Permanent increase of the low-field intensities of (a) the G peak and (b) the D peak. Data in panels a and b are recorded at the same runs as panels b and c of Figure 1. (c) Dependence of the Raman G-peak intensities on the electric field ( $E_{ext}$ ). (d) Permanent decrease in sample conductance is measured, and it does not recover after the electric field is released.

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Parts a and b of Figure 2 show the Raman peaks recorded immediately after releasing each external field used for the measurements shown in parts b and c of Figure 1. The recovery of the G and D peaks to their original frequencies is evident. Peak intensities not only recover but also increase slightly compared to their pristine value before field application. From the data in Figure 2a,b we conclude that the observed effects on the G and D peaks are indeed reversible. The data from Figures 1b and 2a are summarized in Figure 2c, showing the ratios between the intensity of the G-bands



**Figure 3.** Schematics of (a) intratube processes (mostly related to electron—phonon interaction) and (b) intertube processes (related to cross links of different SWNTs) in determining relaxation times. Intratube processes control the performance of individual SWNTs. Intertube processes prevail in SWNT films where each m-SWNT (depicted in black) is cross linked by many other nanotubes, including semiconducting ones (depicted in red).

before and after the external field release for the samples 87 and excitation energies investigated in this study. 88

While the Raman effects in our experiments are reversible, 89 the conductance does not recover after the external field 90 release (Figure 2d). Similar decrease in conductance has been 91 found to improve the on/off ratio of thin film transistors and 92 claimed to be due to burning of metallic SWNTs.<sup>4-7</sup> In our 93 study, the reversibility in decrease of the peak intensities 94 rules out the burning of large amounts of SWNTs. We 95 corroborate this by analyzing the radial breathing mode 96 (RBM) of (*n*,*m*)-SWNTs in our films, as discussed below. 97

It is tempting to assign the observed downshifts to voltage-98 induced Joule heating, increasing the temperature of the 99 films. Although alternative hypotheses can be easily dis-100 missed,<sup>14</sup> it is crucial to clarify the origin and the amount of 101 Joule heating itself, which must be expectedly large in order 102 to justify the observed behavior. It was calculated<sup>15</sup> that 103 strong selective heating of Raman-active phonon modes (up 104 to  $T \sim 10^4$  K in *individual* metallic SWNTs) occurs in the 105 presence of current due to Kohn anomalies.<sup>16</sup> Figure 1, 106 however, shows that the linewidth of the G and D bands 107 does not appreciably increase with electric field, as it would 108 do in the presence of a strong increase in phonon temperature. 109 Therefore, we will discuss our results in terms of moderate 110 Joule heating in the presence of Kohn anomalies in an 111 adiabatic system dominated by intertube interactions. This 112 leads to strong electric-field-dependent fluctuations in the 113 dielectric response of SWNT films, with the same mechanism 114 leading to fluctuations of the Raman frequencies in ferro-115electrics.<sup>11</sup> 116

Let us first recall that in percolating SWNT networks, the 117 electronic confinement is released and the wave functions 118 extend over several SWNTs, both semiconducting (s-119 SWNTs) and metallic (m-SWNTs), and  $\tau$ , the Drude 120 relaxation times, depend on the network density and not on 121 intrinsic properties of SWNTs.<sup>2</sup> The intra- and intertube 122 processes for an individual SWNT and a network of SWNTs 123 are schematically shown in Figure 3a,b. In a system where 124 both intra- and interparticle processes contribute to the 125transport mechanisms and the relaxation of electron mo-126 127

menta, the effective relaxation time can be written according

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to Matthiessen's rule<sup>17</sup> as

$$\frac{1}{\tau} = \frac{1}{\tau_{\rm INTRA}} + \frac{1}{\tau_{\rm INTER}} \tag{1}$$

129 where  $\tau_{\text{INTRA}}$  and  $\tau_{\text{INTRR}}$  represent the intratube and intertube 130 relaxation times, respectively. Therefore,  $\tau$  is dominated by 131 the shorter of  $\tau_{\text{INTRA}}$  or  $\tau_{\text{INTRR}}$  which, in SWNT thin films 132 where each tube is interconnected to many others, is clearly 133 the latter. Relaxation indicates that the external field displaces 134 the Fermi sphere through a shift in momentum  $\hbar\Delta k^{18}$ 

$$\hbar\Delta k = e \cdot \tau \cdot E_{\text{ext}} \tag{2}$$

135 where e is the electron charge.

Let us now recall that the strong Raman activity of the G 136 and D bands of metallic SWNTs should correspond to 137 exceptionally strong electron-phonon coupling,<sup>3,10,19</sup> whose 138 origin had been unclear for a long time. Recently, Piscanec 139 et al.<sup>16</sup> offered an explanation through demonstration of the 140 existence of Kohn anomalies in the screening of ions in 141 metallic graphitic materials. In general, Kohn anomalies 142occur when the size of the Fermi surface is comparable to 143the phonon wavevector  $\mathbf{q}$ .<sup>16,20–22</sup> As discussed by Piscanec 144 et al.,<sup>16</sup> the  $\pi$  and  $\pi^*$  bands in graphite and m-SWNTs touch 145the Fermi level  $(E_{\rm F})$  at the **K**-point which results in a very 146 small Fermi wavevector ( $k_F \sim 0$ ) whose modulus approaches 147those of the G and D phonon wavevectors ( $\mathbf{q} = \mathbf{\Gamma} = \mathbf{0}$  and 148 $\mathbf{q} = \mathbf{q}' - \mathbf{K} = \mathbf{0}$ ). Since  $|2\mathbf{k}_{\mathbf{F}}|^{-1}$  represents the typical scale 149 length for screening a pointlike disturbance,<sup>22</sup> the condition 150 $\mathbf{q} \sim 2\mathbf{k}_{\mathbf{F}} \sim \mathbf{0}$  requires that infinite distance is needed for the 151 electrons to fully screen an optical phonon. 152

It is well-known that Kohn anomalies in one-dimensional 153(1-D) solids lead to logarithmic divergence of the static 154dielectric response,  $\epsilon(q \sim 2k_F, \hbar\omega \sim 0)$ , while in 3-D solids 155the divergence only affects the first derivative of this quantity. 156Dealing with 1-D electronic structures, it is then obvious 157 that small fluctuation in the electron momenta (e.g., by 158applying a constant external field) corresponds to strong, non-159 negligible, fluctuation in the dielectric response.23 We shall 160treat such fluctuations in the framework of the Lindhard 161 model.<sup>24</sup> Accordingly, the dynamic dielectric response of the 162anomalously screening electrons in the presence of a change 163 in momentum  $\hbar \Delta k(E_{\text{ext}})$  is given by<sup>22</sup> 164

$$\epsilon[\Delta k(E_{\text{ext}}),\hbar\omega] - 1 = -4e^{2}\epsilon_{0}\lim_{\substack{k_{\text{F}}\to 0\\q/2k_{\text{F}}\to 1}}\int dk \frac{f(k_{\text{F}} + \Delta k + q/2,T) - f(k_{\text{F}} + \Delta k - q/2,T)}{\epsilon_{k+\Delta k+q/2} - \epsilon_{k+\Delta k-q/2} - \hbar\omega}$$
(3)

where  $\epsilon_0$  is the dielectric response in vacuum and the Fermi-Dirac population probability f(k,T) will be taken to be approximately linear in the energy domain  $E_F \pm k_B T/2$  and 1 or 0 elsewhere. Since the dielectric responses obtained from ellipsometry at our Raman excitation energies ( $\hbar\omega = 1.57$ -

1.92 eV) follow a Drude behavior,<sup>2</sup>  $\in_k$  will be taken to be 170 the dispersion relation for free electrons ( $\in_k = \hbar^2 k^2/2m$ ). 171 Similar conclusions however can be also anticipated when 172assuming a linear band structure for  $\in_k$  as customary for 173individual SWNTs. Care should be taken in evaluating eq 1743, because very slight changes in q,  $\omega$ , and T can lead to 175fluctuations of  $\epsilon(q, \hbar\omega)$  from 1 to infinity.<sup>23</sup> Therefore, since 176 a very small value of  $k_{\rm F}$  is expected in our percolating 177 networks, we estimate eq 3 at  $k_{\rm F}$  tending to zero with the 178 same zeroth order of q, thus leading to a finite ratio  $q/2k_{\rm F}$ 179  $\rightarrow$  1. Evaluation of eq 3 gives  $\epsilon(0, \hbar\omega > 0) - 1 = 0$  in the 180 absence of electric field, while in the presence of field 181

$$\epsilon(\Delta k, \hbar \omega) - 1 = \frac{8e^2}{\epsilon_0 k_{\rm B} T} \left( \sqrt{\frac{mk_{\rm B} T}{\hbar^2} + \Delta k^2} - \sqrt{\frac{mk_{\rm B} T}{\hbar^2} - \Delta k^2} \right)$$
(4)

for

$$k_B T \gg \frac{\hbar^2 \Delta k^2}{m}$$

The intensity and the frequency of the Raman-active 183 optical phonons are related, via the electron-phonon cou-184 pling, to the dynamic dielectric response  $\epsilon(q \sim 2k_{\rm F}, \hbar\omega)$ .<sup>22</sup> 185 Therefore, knowledge of the dynamic dielectric response will 186 now allow us to extract information about the G and D mode 187 frequencies. Especially, if the screening is assumed to 188 (perturbed by temperature and electric field) largely deter-189 mine frequencies of the screened optical phonons, then the 190 Raman shifts in the presence  $[\Omega(E_{ext})]$  and absence  $[\Omega(0)]$ 191 of field can be related by<sup>11,25</sup> 192

$$\Omega_{\rm T}(E_{\rm ext})^2 \cdot \epsilon[\Delta k(E_{\rm ext}), \hbar\omega] = \Omega_{\rm T}(0)^2 \cdot \epsilon(0, \hbar\omega)$$
(5)

The anharmonic modifications of the SWNT structure can 193 be included by assuming a temperature-dependent zero-field 194 Raman shift  $\Omega_{\rm T}(0) \approx \Omega_{300\rm K}(0) - X_{\rm T}T (X_{\rm T} \approx 0.01 \text{ cm}^{-1} \text{ K}^{-1})$ , 195 for the G peak<sup>26</sup>). However, we anticipate that they would 196 not significantly affect the parameters achievable by fitting 197 our model with the experiment (relaxation times and tem-198 peratures change below 30-40%). Replacement of 199  $\epsilon[\Delta k(E_{ext}),\hbar\omega]$  and  $\epsilon(0,\hbar\omega)$  from eqs 3 and 4 into eq 5 leads 200 to the following relation for the frequency of the Raman 201 optical modes upon temperature and external field increase, 202 as plotted in Figure 4a 203

$$\Omega_{\rm T}(E_{\rm ext}) = \Omega_{\rm T}(0) \bigg[ 1 + \frac{8e^2}{\hbar\epsilon_0 k_{\rm B}T} \bigg( \sqrt{mk_{\rm B}T + \frac{e^2\tau^2}{2}E_{\rm ext}^2} - \sqrt{mk_{\rm B}T - \frac{e^2\tau^2}{2}E_{\rm ext}^2} \bigg]^{-1/2}$$
(6)

A comparison between our model and experimental results 204 is shown in Figure 4b,c. Fits were obtained assuming the 205 temperature of the Raman-active phonons rising linearly from 206

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**Figure 4.** (a) Dependence of the Raman shifts on the electric field  $(E_{\text{ext}})$  according to eq 6, assuming that the samples, initially at room temperature  $(T_{\min})$ , heat proportionally with electric field  $(E_{\text{ext}})$ . Comparison with measured (b) G-peak and (c) D-peak frequencies. The lines represent data fits from eq 6 with  $T_{\max} = 600$  K and  $\tau$  as reported in the legend.

 $T_{\rm min} = 300$  K to  $T_{\rm max} = 500-700$  K at external fields  $E_{\rm ext} =$ 207 0-7500 V/cm.<sup>27</sup> Note that these temperatures are far too 208 low to burn the m-SWNTs. Furthermore, strong temperature 209 increase would have been accompanied by broadening of 210 the G, D, and RBM peaks,<sup>26</sup> which we did not observe. Thus 211Joule heating in our films must be moderate, in agreement 212with the relatively low maximum temperatures  $(T_{max})$  pre-213dicted by our model. In the framework of our model, the 214decrease in intensity of the Raman modes can be easily 215 explained since the Stokes/anti-Stokes Raman cross sections 216 $I_{\rm S/AS} \sim |\partial \epsilon / \partial u_{\rm H}|^2 + |\partial \epsilon / \partial u_{\perp}|^{2} {}^{28}$  decrease at increasing fields 217 in direction longitudinal to the field, while remaining 218 unchanged in transversal directions.<sup>29,30</sup> Furthermore our fits 219lead to relaxation times of  $\tau \sim (1-5) \times 10^{-15}$  s, which agree 220 well with the ones achievable by ellipsometry.<sup>2</sup> Such values 221 are of the same order of magnitude to the inverse of the 222G-band pulsation ( $t_{\rm G} \approx 3 \times 10^{-15}$  s). This is in contrast to 223



**Figure 5.** Modifications of the RBMs by external field at (a) 1.96 eV (exciting both m- and s-SWNTs) and (b) 1.57 eV (exciting only s-SWNTs). Assignments of specific (n,m)-SWNTs are taken from Telg et al.<sup>32</sup> The *reversible* decrease for s-SWNTs (red) and the *reversible* increase for m-SWNTs (blue) are shown. In contrast, after field release, the *permanent* effects are always in increasing the RBM intensities for both s- and m-SWNTs at (c) 1.96 eV and (d) 1.57 eV.

what happens in a single graphene layer<sup>20</sup> (or, likely, a single 224individual m-SWNT) where the relaxation times, being 225dominated by intralayer (or intratube) processes, are much 226 longer and  $t_G \ll \tau \approx \tau_{INTRA} \approx 100 \times 10^{-15} \text{ s}^{31}$  leading to 227 the breakdown of the adiabatic Born-Oppenheimer ap-228 proximation. In contrast, the condition  $t_{\rm G} \sim \tau \approx \tau_{\rm INTER} \sim$ 229 $10^{-15}$  s, which still persists in our thin films, leads to a 230 scenario that is still adiabatic and, thus, entirely different 231from the nonadiabatic behavior of the Raman spectra in the 232presence of Kohn anomalies as discussed in ref 20. 233

We have also examined the RBMs of our thin films in 234 order to investigate the influence of the electric field on 235 (n,m)-SWNTs with various chiralities. The RBMs are shown 236 in parts a and b of Figure 5. It can be seen from Figure 5a 237that at  $\hbar \omega = 1.96$  eV, where both s- and m-SWNTs are 238 excited, the intensities of the RBMs of s-SWNTs decrease 239 with increasing electric field while the intensities of the 240 RBMs of m-SWNTs increase. In Figure 5b ( $\hbar \omega = 1.57 \text{ eV}$ ) 241where only s-SWNTs are sampled, the intensities of the 242RBMs decrease with increasing electric field. In contrast, 243after the electric field has been released, it can be seen in 244 Figure 5c,d that the RBM intensity always slightly increases 245in both s- and m-SWNTs. The most interesting feature of 246 this slight increase is that it remains permanent subsequent 247to the field release. Thus, the decrease in measured conduc-248tance shown in Figure 2d cannot be correlated to the claimed 249 preferential elimination of m-SWNTs. 250

The increase in intensities of the RBMs of m-SWNTs is 251 an expected effect if the increase in Boson number of the 252

optical phonons is the determining factor of peak intensity. 253The decrease in the intensities of RBMs in s-SWNTs is not 254consistent with Joule heating as the determining factor in 255controlling the intensity of the RBMs. Indeed, it can be 256demonstrated<sup>14</sup> that the decrease in RBM intensities cannot 257be accounted for by assuming that all the m-SWNTs are 258moving closer to resonance, while all the s-SWNTs are 259 moving off resonance. Upon a temperature increase, the 260261 resonant energies<sup>32</sup> of some of our (n,m)-SWNTs are expected to be closer to the Raman excitation energies, 1.57 262 and 1.96 eV, while other (n,m) tubes will be farther from 263 their resonant energies.<sup>14</sup> However this would happen without 264any systematic dependency on the metallic or semiconducting 265nature of each (n,m)-SWNT.<sup>14</sup> Rather, we suspect that the 266 intensity decrease of the RBMs of s-SWNTs at increasing 267 voltage are more likely to be related to the same causes 268 determining the decrease of the D- and G-peak intensities. 269

270 In conclusion, we reported on the changes in Raman peaks 271of SWNT thin films as a function of an external electric field. We assign such effects to anomalous electron-phonon 272interactions. We dismiss the idea that, in SWNT thin films, 273voltage pulses produce Joule heating high enough to burn 274large amounts of m-SWNTs. This does not happen because 275276 the maximum temperatures reached in SWNT thin film devices under voltage application are much lower than in 277individual SWNT devices, and the relaxation times are much 278shorter. Rather, thermal oxidation,<sup>33</sup> selective cutting of the 279m-SWNTs, or elimination of very small amounts of m-280 281 SWNTs on some critical percolating pathways may reduce the "off" currents and improve the transistor performance. 282Finally, electrical Raman spectroscopy will be a new and 283powerful technique for characterizing thin films and devices 284incorporating one-dimensional nanostructures. 285

Supporting Information Available: Discussions of the 286 difficulties of interpreting experiments in terms of electro-287mechanical strain and the origin of the voltage dependency 288 of the RBM intensities. This material is available free of 289 charge via the Internet at http://pubs.acs.org. 290

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- (23) For instance, at T = 0 K, eq 3 would lead to  $\epsilon(\Delta k, \hbar \omega) 1 \sim \log\{[(x + \delta \omega)^2 1)]$ 318  $(x_{\rm E} + y)^2 - (x_{\rm E} + y)^2]/[(x - 1)^2 - (x_{\rm E} + y)^2]$ , with  $x = q/2k_{\rm F}$ ,  $x_{\rm E} = q/2k_{\rm F}$ 319  $\Delta k(E_{\rm ext})/2k_{\rm F}$ , and  $y = m\omega/\eta q$  so that Kohn anomalies (x = 1) 320 correspond, in the absence of field, to an infinite static response  $\epsilon(0,0)$ 321 $-1 \rightarrow \infty$  and a null dynamic response  $\epsilon(0, \hbar\omega) - 1 = 0$  while, in 322 the presence of field,  $\epsilon(\Delta k, 0) - 1 \rightarrow \infty$ . 323 324
- (24) Actually, the use of the Lindhard model relies on the adiabatic Born-Oppenheimer approximation which, as verified below, still holds in 325our SWNT thin films. In contrast, our adiabatic model will be 326 inadequate in nonadiabatic systems (e.g., graphene).
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- (27) The relaxation times determined within our model are of the order 337 of magnitude available in literature (see ref 22, p 10). Furthermore, 338 straightforward Drude analysis of the ellipsometry spectra of our 339 samples (ref 2) also leads to  $\tau \sim 10^{-15}$  s. We suspect that especially 340 intertube processes between one m-SWNT and one s-SWNT are 341342 important in lowering the relaxation times, since s-SWNTs may act as thermal sink (ref 15). Thus, the higher the participation of 343 s-SWNTs to electrical transport, the smaller  $\tau_{INTER}$ . Impurities might 344 also contribute in decreasing both intra- and intertube relaxation times. 345346
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